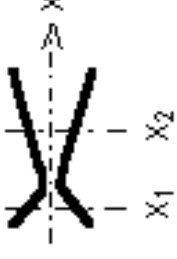


The **analysis of compressible fluid flow** involves four equations of particular interest:  
 Energy - Continuity - Momentum - The equation of state

Conservation of energy, isentropic flow (no heat exchange, no friction) between  $x_1$  and  $x_2$ :

$$h_1 - h_2 = \frac{1}{2}(v_2^2 - v_1^2) = C_p(T_1 - T_2) \quad [\text{eq. 1}]$$



Enthalpy  $h$ ,  $v$  velocity in  $x$ -direction,  $C_p$  heat capacity,  $T_1$ ,  $T_2$  temperatures at  $x_1$ ,  $x_2$ .

Change (decrease) in enthalpy is equal to the change (increase) in kinetic energy

- heat of the fluid is being used to accelerate the flow!

For isentropic flow: temperature, pressure, and fluid density  $\rho$

$$\frac{T_0}{T} = \left(\frac{P_0}{P}\right)^{\frac{k-1}{k}} = \left(\frac{\rho_0}{\rho}\right)^{k-1} \quad [\text{eq. 2}], \quad \text{with } k: \text{ ratio of specific heats} \quad k \equiv \frac{C_p}{C_v} = \frac{C_p}{C_p - R}$$

and  $R = R'/\text{mol.weight}$ ,  $R'$ : Avogadro's constant